EECE455 – Project #3

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Official Description from Dr. Ali El Hussein

Project-3. Polynomial Arithmetic (More Challenging; More Grades)

The code will allow a user to perform arithmetic on polynomials in $GF(2^m)$ with m = 163. The operations to be performed are modulo reduction, finding the inverse, addition, subtraction, multiplication, and division.

The implementation should be modular and can be easily extended to other standard powers such as: 163, 233, 239, 283, 409, 571.

The software should allow inputs and display outputs in either Binary or Hexadecimal.

Introduction:

This app is a GF(2^m) calculator currently supporting $2 \le m \le 514$ and m=571 (m is an Integer). It can add, subtract, multiply, divide, inverse and reduce (apply modulo of irreducible polynomial). It can take Binary input or Hex input and display the result of the operation in decimal, binary and hex.

In the submitted zip, we will have the code in an archive file, and an executable.

Please make sure to disable any anti-virus, so that the executable can run properly.

Please view our demo video where we detail how to run the program in 2 methods: <u>https://youtu.be/k2099KMwW8A</u>

GUI:

Push buttons on the left side of the app, each button specifies what it does (add, subtract, multiply, divide, inverse, reduce)

Input boxes on the right with labels to their left specifying what they do. You can input either binary or hex in their respective input boxes. The app will give a warning when you input hex and binary so will only operate on either 2 hex or 2 bin but not one hex one bin, or for improper input format or improper input combinations (add takes 2 inputs; inverse takes one input; cannot divide by 0; binary1 improper input...)

The results are displayed in 3 formats: Decimal, Binary, and Hexadecimal.

The irreducible polynomial used is also displayed.

Backend:

We used: https://pypi.org/project/galois

We used the previously mentioned Galois module to find all irreducible polynomials up to $GF(2^{514})$ and store them in a JSON file.

When doing an operation, the app now is pretty much instantaneous since it does not have to calculate the irreducible polynomial, it just looks it up in the JSON file which is very quick.

After checking the inputs and making sure everything is the way it should be, the operation function is called (depending on what button was pressed: add or sub or mul or...), if the inputs are outside the Galois field specified by the user, the inputs will be reduced and then the function called will be done. Using NumPy to operate on the polynomials and then reducing them appropriately we implemented each operation.

Some Screenshots of the app:

Ø Galois Polynomials Calculator ٥ \times Polynomial1 in binary 11 1 Polynomial2 in binary Polynomial1 in HEX Polynomial2 in HEX 8 GF(2^m); m= esult Decimal: Copy Dec Value Copy Bin Value Binary: Hexadecimal: Copy Hex Value Irreducible Polynomial: $x^{8} + x^{4} + x^{3} + x^{1} + x^{0}$ 🛱 🛜 🗮 💼 🦧 🍋 🛇 🛍 🥖 🏘 1/ D: 14.38 kB/s ^ 🗃 🖉 🖬 (23.4 PM 12/10/2021) ${\cal P}$ Type here to search

Addition:

Division:

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Sub	Polynomial2 in b	inary					10												
Mul	Polynomial1 in	HEX																	
Div	Polynomial2 in	HEX																	
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Red																			
	Results			2		_						^							
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Division with hex input:

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Mul	Polynomial1 in HEX	A
Div	Polynomial2 in HEX	2
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Red		
	Results	5
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	Binary:	0b101 Copy Bin Value
	Hexadecimal	0x5 Copy Hex Value
	Irreducible Polynomial:	x^512 + x^8 + x^5 + x^2 + x^0
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Inverse:

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Sub	Polynomial2 in binary			
Mul	Polynomial1 in HEX			
Div	Polynomial2 in HEX			
Inv	GF(2^m); m=	14		
Red				
	Results	246		
	Decimal:	Copy Dec Value		
	Binary:	Ob1110110 Copy Bin Value		
	Hexadecimal:	Copy Hex Value		
	Irreducible Polynomial:	x^8 + x^4 + x^3 + x^1 + x^0		
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One warning:

Galois Polynomials Calculator Help		- 0 ×
Add Polynomial1 in binary Sub Polynomial2 in binary Mul Polynomial2 in HEX Div Polynomial2 in HEX Inv Inv Red OK		
Decimal:		Copy Dec Value
Binary:	0b10 0x2	Copy Bin Value
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Irreducible Polynomial:	$x^{A}8 + x^{A}4 + x^{A}3 + x^{A}1 + x^{A}0$	
🕂 🔎 Type here to search 🛛 🛱 👩 🗖	💼 🧠 🍋 😵 🛍 🚄 🏘 🖉 U: 67. D: 160	76 k8/s へ 53 0 📼 🦟 (小) ENG 12:34 PM 41 k8/s へ 53 0 📼 🥂 (小) ENG 12/10/2021 - 100